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MEASUREMENTS OF THE WATER SURFACE  
CONTOUR BEHIND A HYDROFOIL  
OF MODERATE ASPECT RATIO

by  
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Pasadena, California

Report No. E-110.4

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## SUMMARY

An experimental program has been carried out for the measurement of the water surface contour due to a submerged hydrofoil of finite span. Because of the hydrofoil downwash, the water surface has a rather pronounced depression in the form of a long, narrow trough which extends many chords aft the hydrofoil. When the trailing vortex cores becomes sufficiently close to the water surface depression, flash ventilation of the vortices and the entire upper surface has been observed to occur abruptly.

The model used here was a hydrofoil with a NACA 16-206 section and a rectangular plan form, mounted on a NACA 16-006 strut. The hydrofoil has a chord of 3 inches and an aspect-ratio of 1.33. It has been found that the length and depth of the surface depression, and the location of the trough bottom are well defined functions of the Froude number and of the ratio of chord-to-submergence depth. It has also been observed that the distance between the trailing vortex core and the lowest points of the depression is an important parameter in effecting the onset of ventilating flow. This investigation covers a range of flow velocity, angle of attack, depth of submergence, and the flap angle deflection.

## TABLE OF CONTENTS

Nomenclature	iii
Introduction	1
Experimental Setup	2
Discussion of Results	4
Conclusions	6
References	8

### Nomenclature

$h$	depth of submergence with respect to leading edge of the hydrofoil (ft. )
$d'$	maximum surface depression with respect to undisturbed surface (ft. )
$L$	lift force
$\ell$	longitudinal or downstream distance from leading edge (ft. )
$w$	transverse distance from hydrofoil mid-span (ft. )
$c$	hydrofoil chord = 0.25 ft.
$V$	water velocity (fps)
$Fr = \frac{V}{\sqrt{gc}}$	Froude number based on chord
$\alpha$	angle of attack (deg)
$C_L$	lift coefficient

## 1. Introduction

In the development of hydrofoil systems operating near the free water surface, it is important to determine the effects of the free surface on the basic characteristics of hydrofoil performance. Other than its effects on the lift, wave drag, moment of force of a hydrofoil, the free surface has an additional important effect on the change of the basic flow configuration by the inception of cavitation and ventilation about the hydrofoil. The formation of an air bubble by ventilation at the tips and upper surface of a submerged flat plate has been shown and discussed by Wadlin, Ramsen and Vaughan (1)\*. It was reported that when the flow velocity past a hydrofoil, held at high angles of attack and submerged at shallow depths, is sufficiently large, air was observed to enter the trailing vortices from downstream. As the speed was increased the entrained air proceeded forward along a helical path inside the vortices until it reached the model, causing the entire upper side to be ventilated.

Similar observations have been made at this Hydrodynamics Laboratory using a hydrofoil with a NACA 16-206 section and a rectangular plan form. A 16mm motion picture (Ref. 2) presents some typical observations and experimental results, showing the effect of speed, angle of attack, operating depth and flap angles on the ventilation characteristics.

These experimental observations showed that due to the hydrofoil downwash, the water surface had a rather pronounced depression in the form of a long, narrow trough which extended many chords aft the hydrofoil, but before the well known wave pattern would be established further downstream. The results gave evidences that this water surface depression was very important to the initiation of ventilation. Apparently, this surface depression brings the free surface closer to the trailing vortices which represent a low pressure region (compared with

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\* Number in parenthesis indicate the references at the end of text.

the ambient) in the flow; hence air bubbles tend to migrate from the surface to the low pressure field of the tip vortices. When the depth of submergence was sufficiently small, and these vortex cores sufficiently close to the surface depression, flash ventilation of the vortices and the entire upper surface was observed to occur abruptly.

As was pointed out in Ref. (1) and later in (3), when the upper surface becomes ventilated, the lift of the hydrofoil suddenly drops by as much as 45 percent. This loss in lift and the large downstream disturbances produced by the trailing cavities are the important reasons for studying this phenomena from the standpoint of engineering application. The problem is also of interest in view of the determination of the critical conditions for ventilation inception and its bearing on related free-boundary flows. Consequently, it was decided to explore in a systematic manner the mechanism and conditions under which this type of ventilation takes place.

The first part of these studies involved the determination of the water surface contour behind a hydrofoil. Three important parameters --depth of submergence, velocity, angle of attack--were considered in this experimental program. Aspect ratio, though it can be important, was kept fixed in this study. Measurements were made of the surface contour, and in particular, the magnitude and location of the maximum surface depression were recorded for several velocities, angles of attack and foil depths.

## 2. Experimental Setup

The hydrofoil used in this experimental program was the NACA 16-206 section without flap. The chord of the hydrofoil was three inches and the span four inches; hence the aspect ratio was  $4/3$ . There was no taper and the tips were square and parallel to each other. The foil was mounted at mid-span on a ten inch long strut which had a NACA 16-006 section profile and a chord of 2.25 inches. Table I shows the coordinates of the strut and foil.

The model was tested in the Free-Surface Water Tunnel which



has a test section 20 inches wide and eight feet long. The water depth under normal operating conditions is about 20 inches. Although it was recognized that the water surface contour could be a sensitive function of channel depth, width, and velocity, the effect of changes in channel geometry were not explored in these preliminary experiments. Figure 1 shows the apparatus used in this program. The model was supported from an elevating mechanism which permits the model to be positioned vertically with a repeatability of 0.001 feet. The water surface contour was determined with a depth gage which could be positioned at various distances behind and to the side of the model. The longitudinal distance,  $l$ , was measured from the leading edge of the hydrofoil and the transverse distance,  $w$ , was measured from the centerline of the model. The reference level of the surface was taken to be the water surface in the absence of the model. This reference surface was determined with the depth gage for each run with a different velocity, since the water surface level is affected slightly by the tunnel speed. The reference depth of the foil was determined during each run by lowering the model to the water surface until the trailing edge just touched the water surface. A correction of  $\Delta h = c \sin \alpha$ , where  $c$  denotes the chord and  $\alpha$  the angle of attack, was applied to account for the vertical distance between the leading and trailing edges of the hydrofoil. Thus the reference position of the hydrofoil depth is taken to be the distance from the leading edge to the undisturbed water surface at all times.

The water surface contour was measured for the velocity  $V$  equal to 10, 15, 20, and 24.5 feet per second, with angle of attack  $\alpha$  held at 2, 4, and 8 degrees, and depth-to-chord ratio set at 1.0, 0.5, and 0.25. Figures 4 through 8 show the resulting contours to scale. The maximum water surface depression  $d'$ , was investigated further for a large number of foil depths and also for  $-4$  degrees angle of attack. These results are shown in Figs. 9 and 10. Figure 11 shows the relationship between water depth and Froude number and also the lift coefficient. This lift coefficient data was obtained from Ref. (3), which presents the results of a test program conducted with the present hydro-



foil in the Free-Surface Water Tunnel.

### 3. Discussion of Results

The effect of foil submergence on the extent of the water surface displacement is most significant. This effect is seen in the photographs of Fig. 3 and in the measured surface profiles of Fig. 4. This latter figure is drawn to scale for a velocity of 15 fps and  $8^\circ$  angle of attack. It shows how the water surface at the centerline gradually slopes downward to a point which is about eight chords aft the leading edge of the hydrofoil. At 15 fps, this is the observed position of the maximum surface depression for all depths of submergence tested with this hydrofoil model. Downstream of this location the surface rises up again and begins to form a "rooster tail" at the centerline. The graphs of Figs. 5 and 6 give further information on the effect of angle of attack and the Froude number on the surface contour. The transverse profiles in Fig. 7 show how the rooster tail downstream of the hydrofoil develops. The growth of the rooster tail along the centerline is particularly noticeable at a velocity of 10 fps and, as can be seen, it rises above the undisturbed water level. This same phenomenon also occurred at higher velocities, but it took place further downstream (at the entrance of the tunnel diffuser) where it could not be measured.

The effect of angle of attack on the water surface profile is illustrated in Fig. 5. Again the maximum depth of the surface depression occurred eight chord lengths aft of the leading edge. Thus it seems that the longitudinal location of the maximum surface depression depends only on the velocity or, rather, on the Froude number based on chord. It is interesting to note also that the rooster tail formed only at moderate and high angles of attack; for the angle of attack about 2 and 4 degrees, the water surface tended to smooth out very gradually far downstream.

Figure 6 shows the effect of velocity on the longitudinal surface depression for an angle of attack of  $8^\circ$ . At 24.5 feet per second the depth of the water trough became tremendous and extended very

far downstream. For these same conditions the transverse profiles are presented in Fig. 7. Note that the cross sections were taken at regular intervals from the foil leading edge. The star indicates the approximate location of maximum water depth,  $d'$ . Although the length and depth of the surface depression increased with velocity, the width of the trough at the surface as well as at its deepest point was smaller for the high velocities. This is an important result from the standpoint of incipient tip ventilation. As was discussed before, the ventilation was always triggered from this trough, and proceeded forward to the foil tips. When the low local pressure field in the tip vortices becomes so close to the water surface, a passage is formed for the air to enter the vortex. Hence if the distance from these tip vortices to the surface is sufficiently large, ventilation will not occur at all.

In order to determine the effect of model depth, and of angle of attack on the surface depression depth  $d'$  in greater detail, a large number of readings of  $d'$  were taken at small intervals of foil depth. The effect of the Froude number is shown in Fig. 9. The most interesting result here is that the surface depression did not occur when hydrofoil was right at the water surface, but rather when it was somewhat below the surface. In fact, with an increase in the Froude number, the submergence required for maximum surface depression increased also. It should be noted here that the reason for negative surface depression is the fact that the foil depth was measured with respect to the foil leading edge. Hence for the negative values of  $h/c$  the hydrofoil was planing.

The dashed line in this Fig. 9 marks the points at which the tip vortices began to ventilate. When the hydrofoil was raised from a deep submergence toward the free surface, the ventilated tip vortices formed at these points. The ventilation of the entire upper surface occurred after the maximum value of  $d'$  had been reached. This state of ventilation will be called superventilation. The hydrofoil depth at which this superventilation was initiated varied from test to test somewhat and the individual points are, therefore, not marked. There was a considerable hysteresis effect on tip ventilation and superventilation. When the hydro-

foil was lowered below the point of incipient ventilation, after having established ventilation, the cavity would remain for many seconds until all the air had finally entrained and disappeared downstream. In the case of the ventilated tip vortices, the cavity would disappear downstream only when about 1.5 to 2 chords depth was reached. A more detailed study of these effects will be made in the future. Figure 10 illustrates the effect of angle of attack on the maximum depth of the surface depression. It can be seen that the foil depth at which the maximum value of  $d'$  was measured did not change appreciably with positive angles of attack. In the case of  $\alpha = -4^\circ$  the water surface was actually deflected upward. At values of  $h/c$  about 0.1 the lower surface of the hydrofoil became ventilated and a relatively thin sheet of water was scooped up by the upper surface. The large negative value of  $d'/c$  at small foil submergences represents this sheet of water.

The dependence of the maximum surface depth for various submergence ratios is shown as a function of lift coefficient in Fig. 11 and the Froude number in Fig. 12. It is of interest to note from Fig. 12 that the depth-chord ratio is nearly linearly proportional to the Froude number. A theoretical analysis of this depression has been carried out by D. K. Ai and T. Y. Wu, the numerical results of this work will be presented in a future report. It is hoped that this work will explain the salient features of these graphs.

#### 4. Conclusions

From this preliminary experimental study of the water surface contour behind a submerged hydrofoil, the following general conclusions can be made:

- 1) The surface depression is greatest along the centerline at a distance downstream which is directly related to the Froude number.
- 2) The maximum depression of the water surface is nearly linearly dependent on lift coefficient and Froude number.

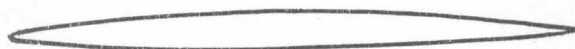
- 3) The maximum depth increases rapidly with a decrease in foil submergence and attains a maximum value between depth-chord ratio of 0.1 and 0.4, depending on the Froude number.

As the hydrofoil approaches the water surface ventilated tip vortices first appear, followed by superventilation when the foil is at 0.1 to 0.2 chords depth. These air entrainment problems will be studied in more detail in the future. It would be of particular interest to determine the conditions for ventilation of the initial vortex and subsequent superventilation, and the conditions under which the ventilated cavity will disappear again.

## REFERENCES

1. Wadlin, K. L., Ramsen, J. A., Vaughan, V. L., Jr.: "The Hydrodynamic Characteristics of Modified Rectangular Flat Plates Having Aspect Ratios of 1.00, 0.25, and 0.125 and Operating Near a Free Water Surface", NACA Report 1246, 1955.
2. Brentjes, J.: "Ventilation Characteristics of a Parabolic and NACA 16-206 Hydrofoil", 16 mm Sound Motion Picture No. 62, Contract Nonr-220(43), Hydrodynamics Laboratory, California Institute of Technology, 1962.
3. Brentjes, J.: "Experimental Force Investigation of a NACA 16-206 Hydrofoil in the California Institute of Technology Free Surface Water Tunnel", Boeing Document D2-11597, Boeing Company, Seattle, Washington, July, 1961.

TABLE I

HYDROFOIL AND STRUT COORDINATES

NACA 16-206



NACA 16-006

NACA 16-206				NACA 16-006	
HYDROFOIL				STRUT	
$X_u$	$Y_u$	$X_l$	$Y_l$	$X$	$Y_u, Y_l$
0.	0.	0.	0.	0.	0.
0.0362	0.0225	0.0383	0.01611	0.0281	0.0145
0.0734	0.0326	0.0766	0.0215	0.0563	0.0203
0.1482	0.0467	0.1518	0.0286	0.1125	0.0282
0.2232	0.0582	0.2268	0.0327	0.1683	0.0341
0.2920	0.0674	0.3018	0.0363	0.2250	0.0389
0.4483	0.0822	0.4517	0.0418	0.3375	0.0465
0.5984	0.0938	0.6016	0.0461	0.4500	0.0535
0.8989	0.1104	0.9011	0.0521	0.6750	0.0610
1.1994	0.1199	1.2006	0.0557	0.5000	0.0659
1.5000	0.1231	1.5000	0.0569	1.1250	0.0675
1.8006	0.1196	1.7994	0.0554	1.3500	0.0656
2.1010	0.1082	2.0990	0.0499	1.5750	0.0593
2.4014	0.0868	2.3986	0.0391	1.8000	0.0472
2.7013	0.0532	2.6587	0.0222	2.0250	0.0283
2.8510	0.0307	2.8499	0.0117	2.1375	0.0159
3.000	0.	3.0000	0.	2.2500	0.0014
L. E. RADIUS = 0.00176"				L. E. RADIUS = .00396	
SLOPE OF RADIUS THROUGH L. E. = .0824					

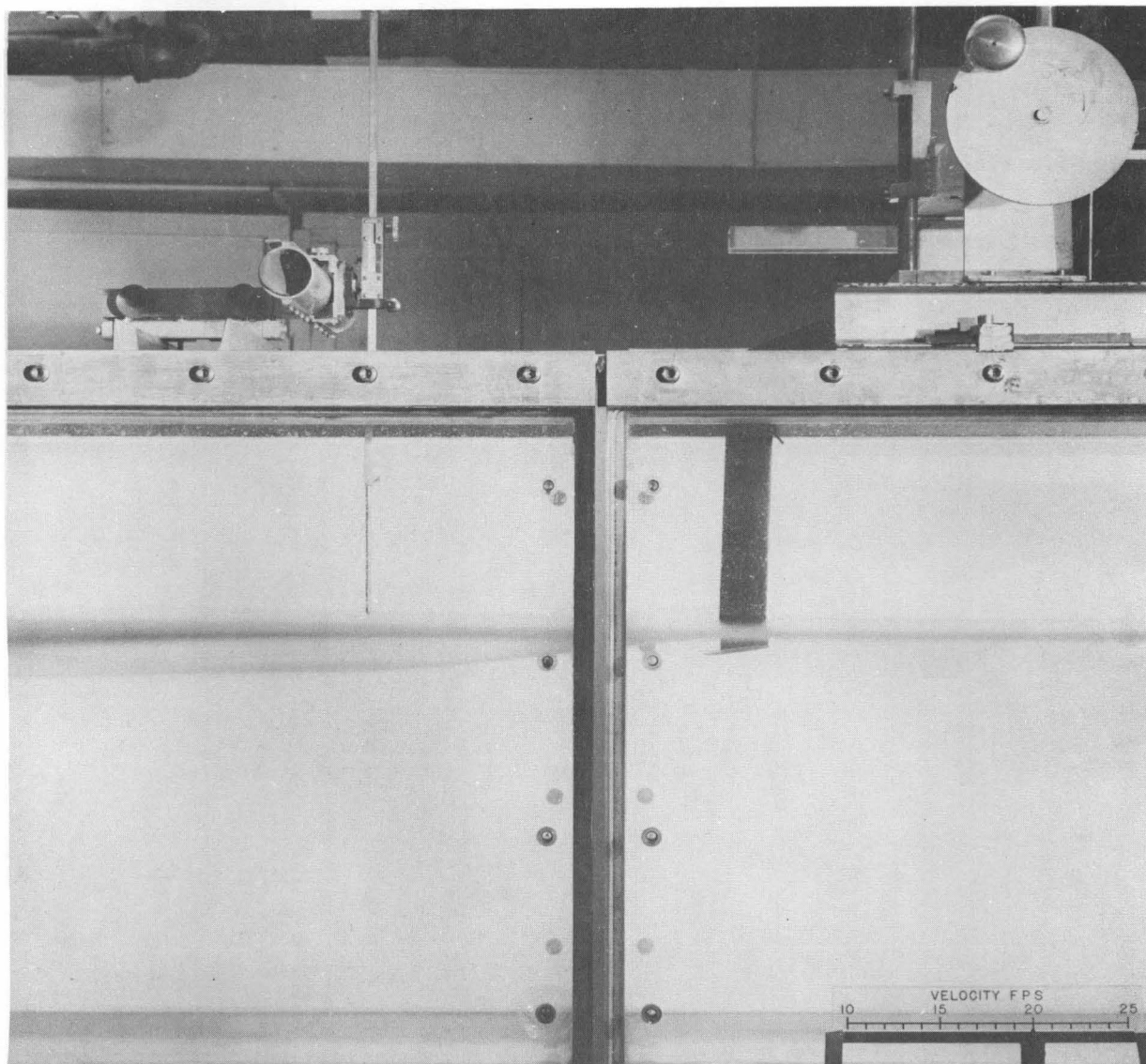
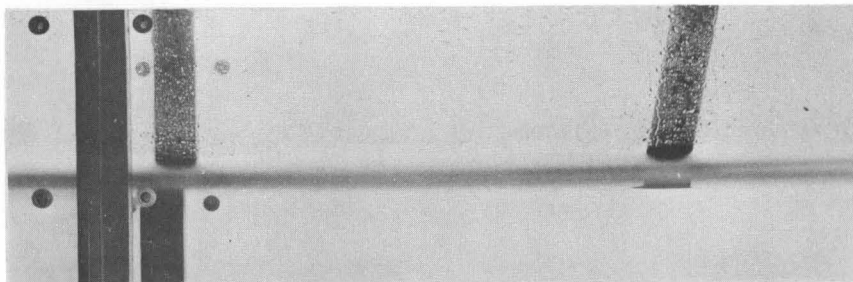
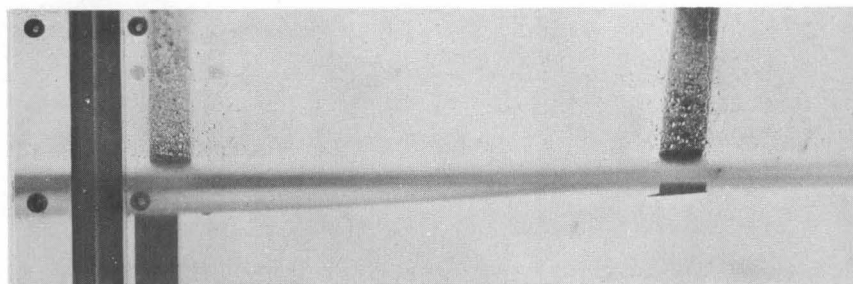


Figure 1. Photograph showing strut-mounted hydrofoil in test section of Free-Surface Water Tunnel. The tunnel velocity is 20 ft. per sec. at an angle of attack of  $8^{\circ}$  and the submergence ratio ( $h/c$ ) is 0.25. The following legend identifies the objects in the photograph: (1) Hydrofoil and strut system, (2) Strut support, (3) Depth gage and traversing mechanism, (4) Velocity indicator.

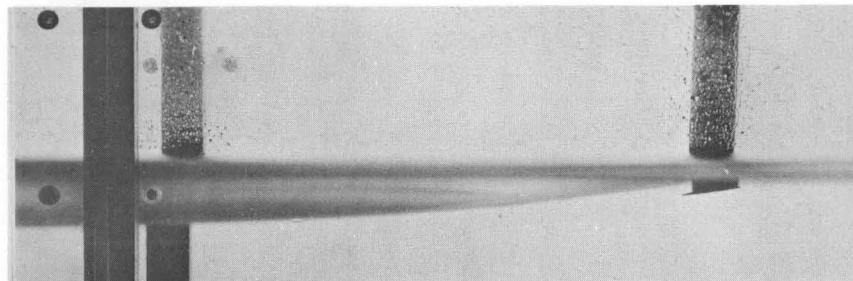




Angle of Attack =  $0^{\circ}$ ,  $C_L = 0.015$

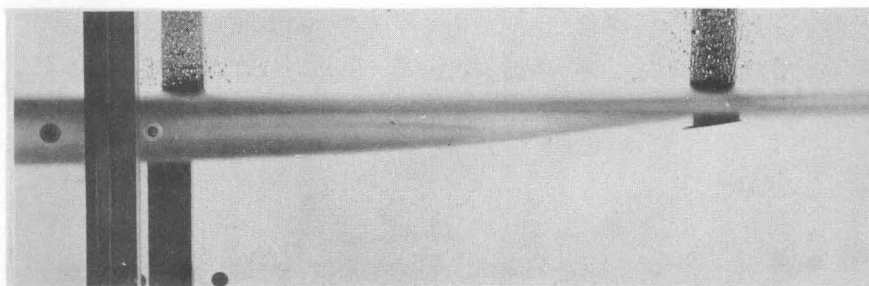


Angle of Attack =  $4^{\circ}$ ,  $C_L = 0.120$

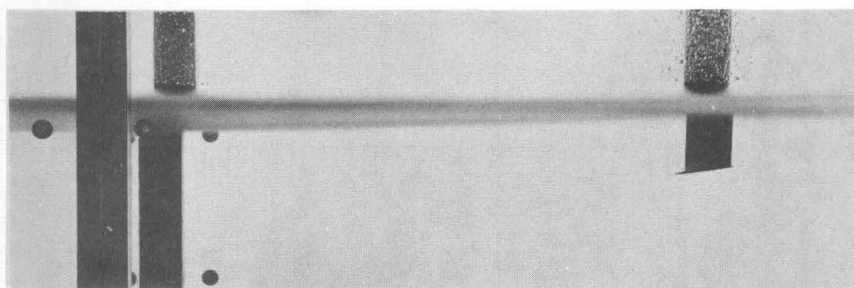


Angle of Attack =  $8^{\circ}$ ,  $C_L = 0.232$

Figure 2. Photographs of water surface depression behind hydrofoil at various angles of attack. The ratio of the submergence to the chord is 0.24 and the velocity is 24 ft. per sec.



$$h/c = .236, \quad C_L = 0.230$$



$$h/c = .98, \quad C_L = 0.323$$

Figure 3. Effect of submergence on the depression of the water surface. In each case the water velocity is 24.5 ft. per sec. and the angle of attack is  $8^\circ$ .

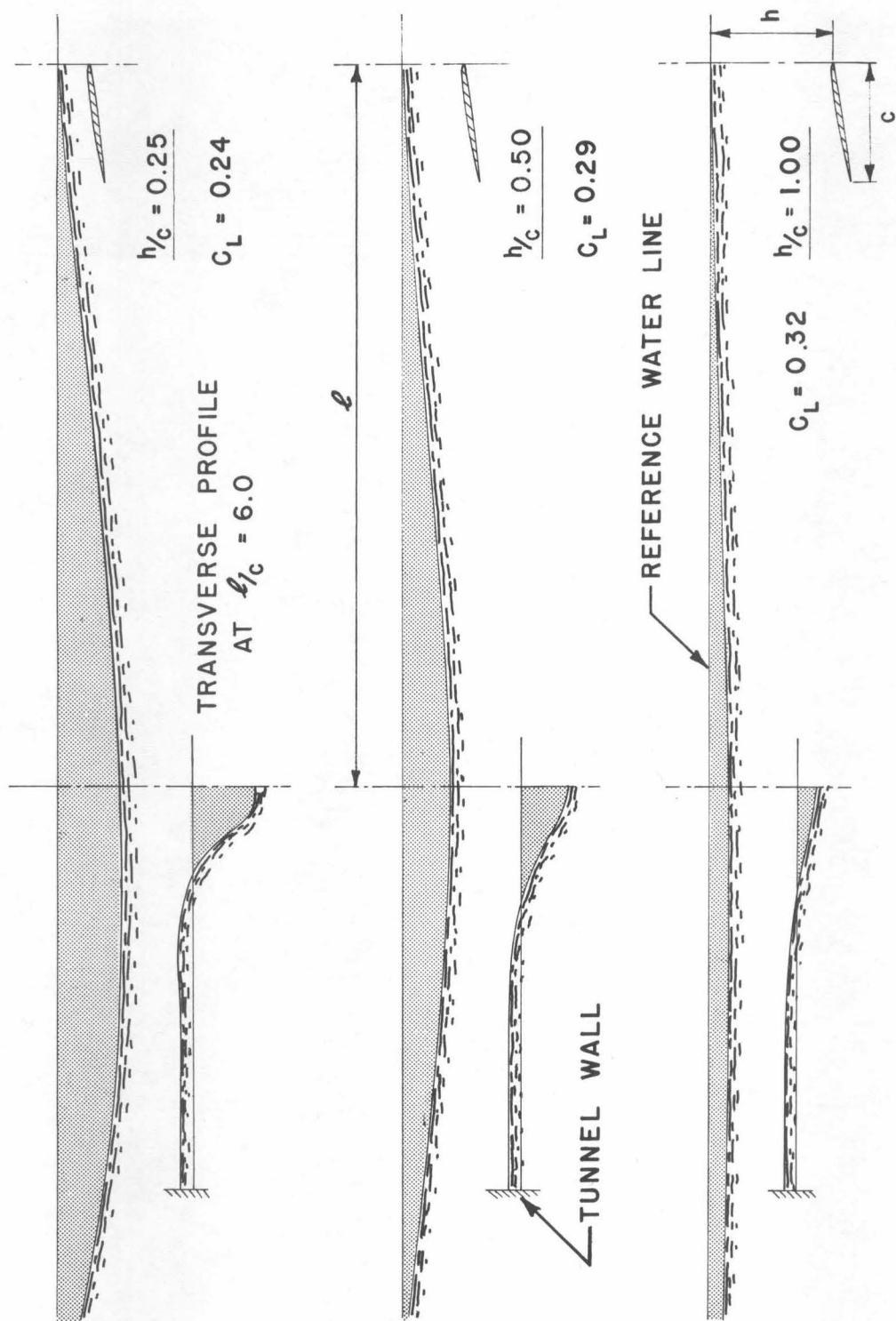


Figure 4. The effect of hydrofoil depth on the water surface profile. The Froude number based on chord is 5.3 and the angle of attack is  $8^\circ$ . For each depth, a longitudinal profile on the centerline of the hydrofoil and a transverse profile six chord lengths downstream are shown. The aspect ratio of the hydrofoil is  $4/3$ .

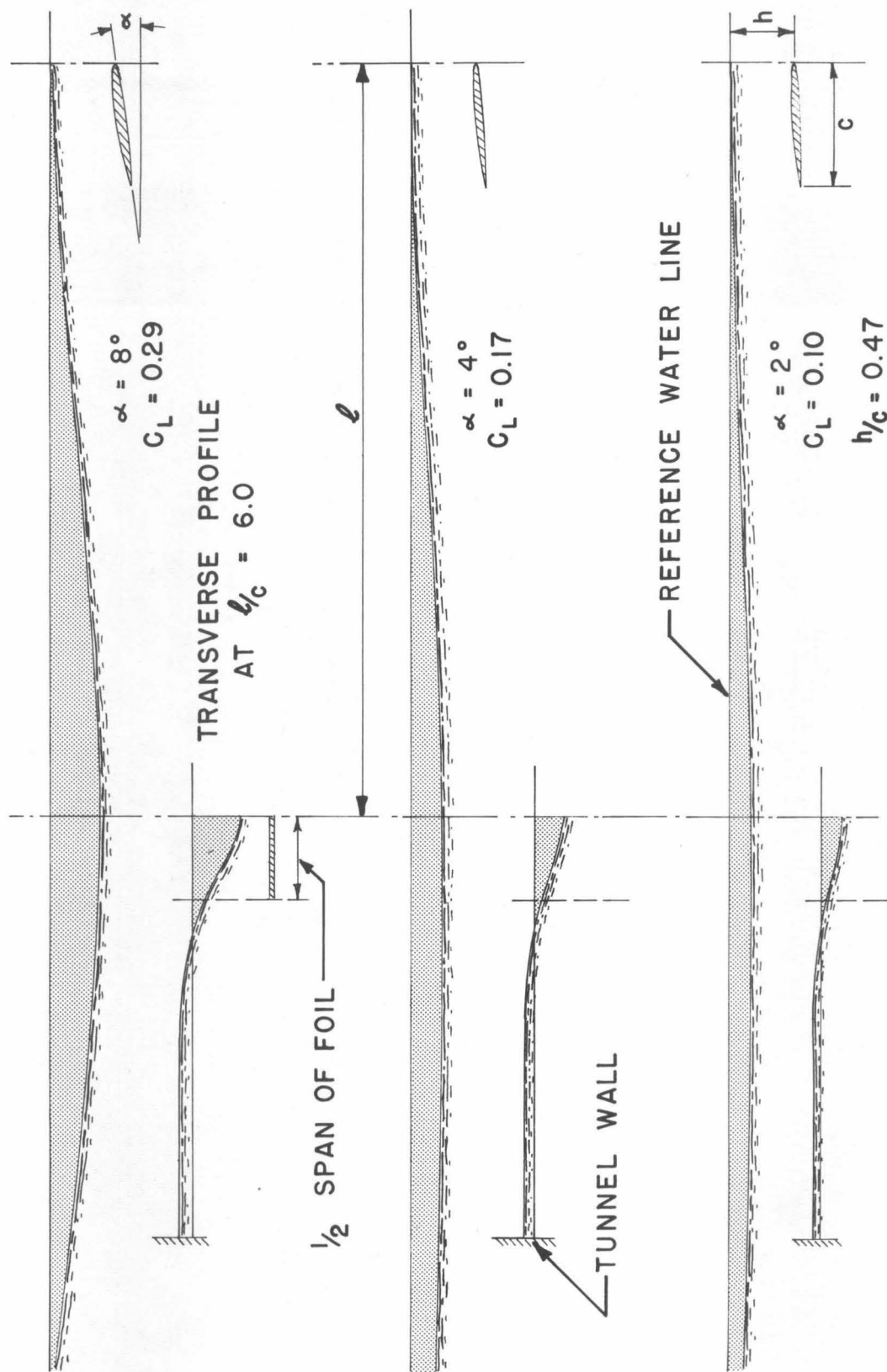


Figure 5. The effect of angle of attack on the water surface profile behind the hydrofoil. The hydrofoil in each case is submerged one-half of its chord length and the Froude number based on chord is 5.3. The aspect ratio of the hydrofoil is  $4/3$ .

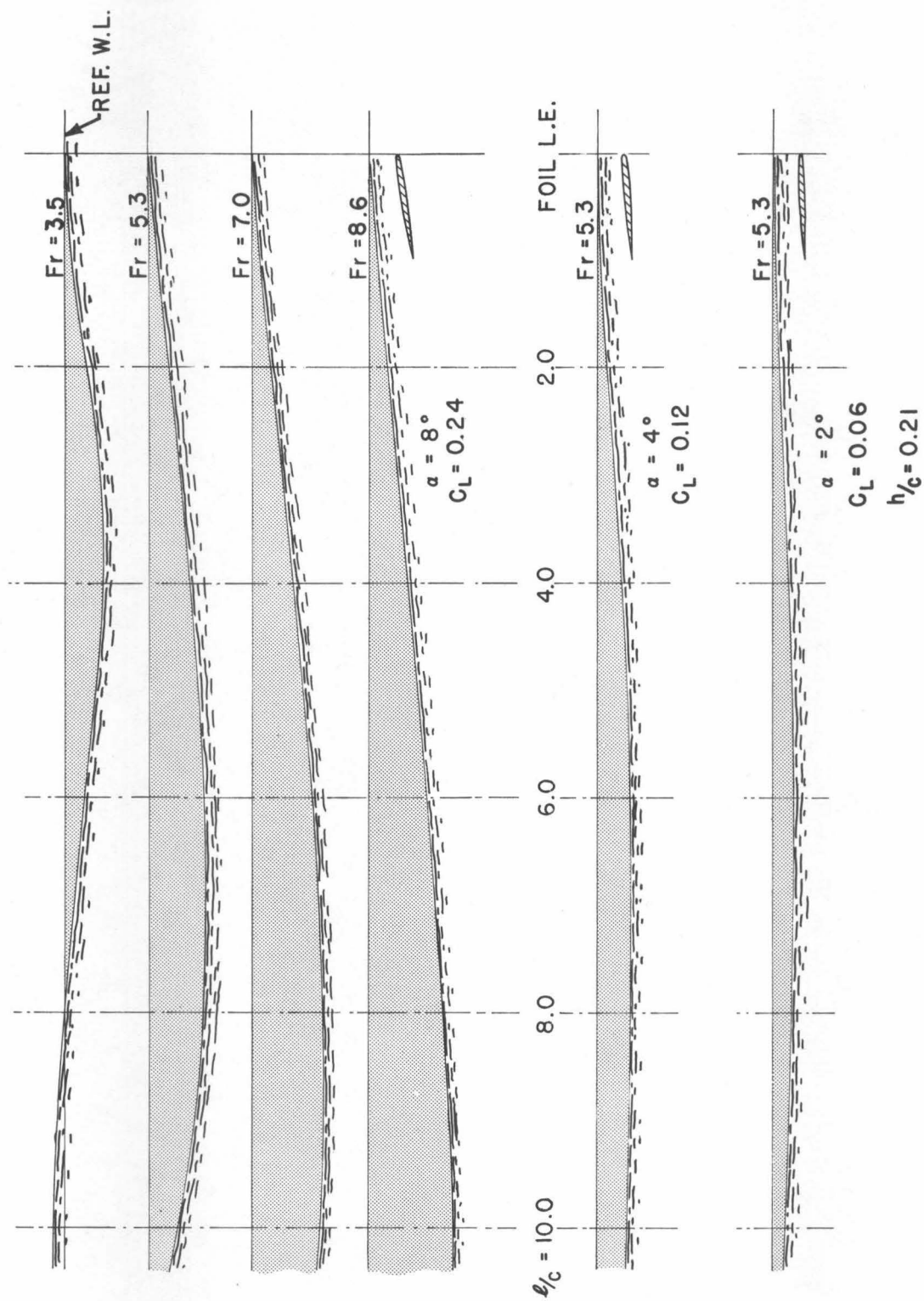


Figure 6. Centerline surface profiles at various angles of attack and Froude numbers at a constant hydrofoil submergence of 0.25 chords.

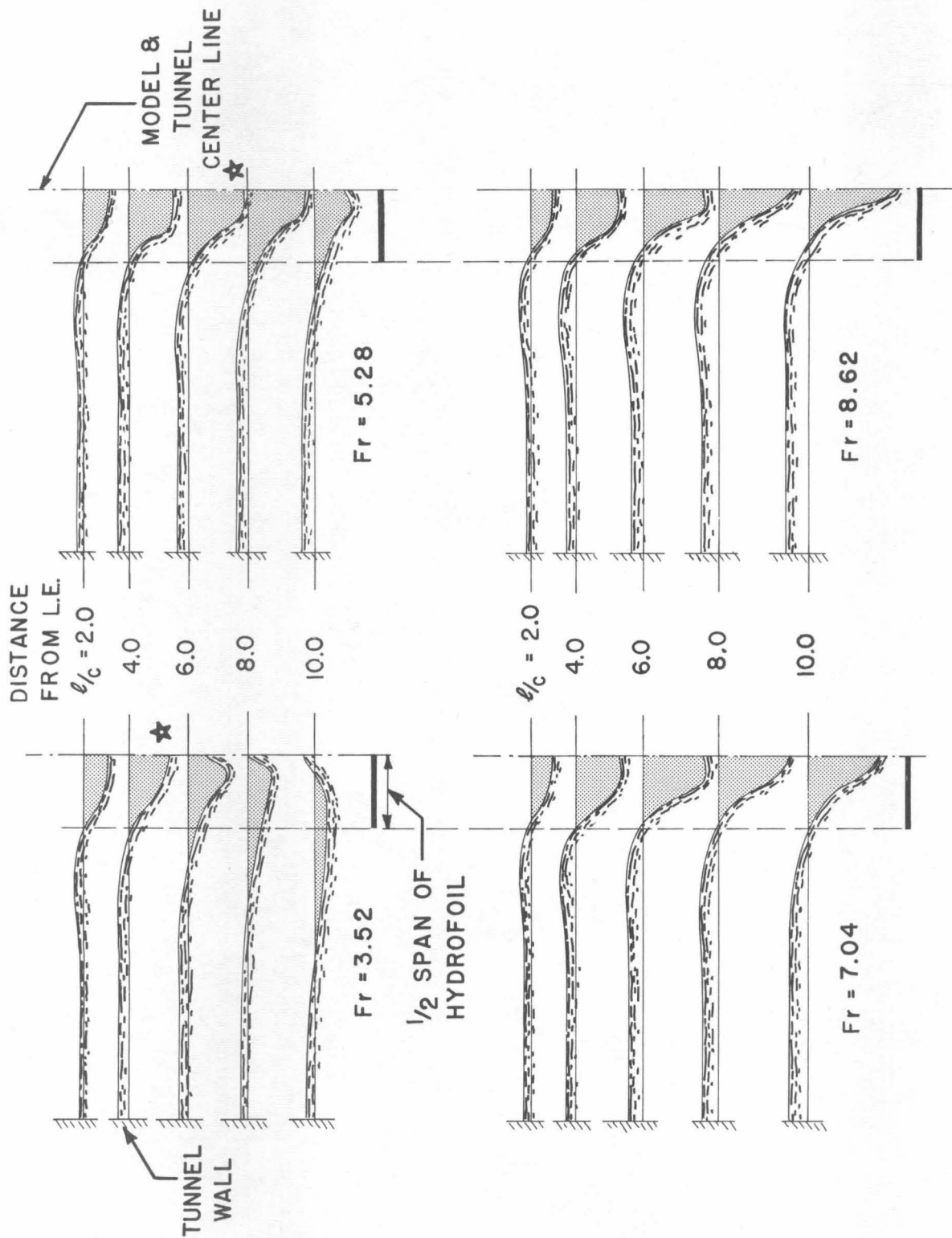


Figure 7. Transverse surface profiles for various Froude numbers at a constant submergence of 0.25 hydrofoil chords and angle of attack of  $8^\circ$ . The "star" on the figure denotes the location of maximum surface depth.

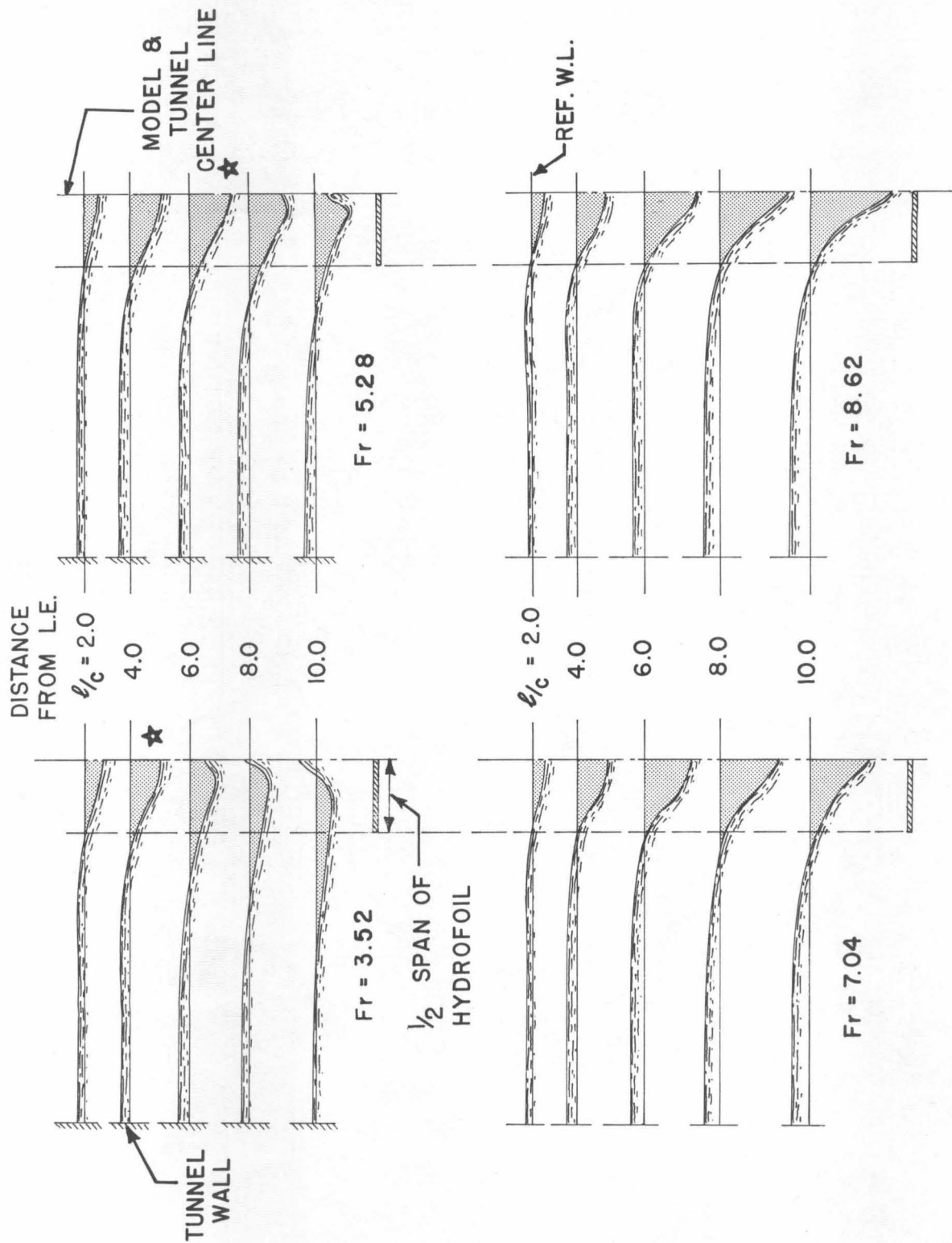


Figure 8. Transverse surface profiles for various Froude numbers at a constant submergence of 0.50 hydrofoil chords at an angle of attack of  $8^\circ$ . The "star" on the figure denotes the location of maximum surface depth.



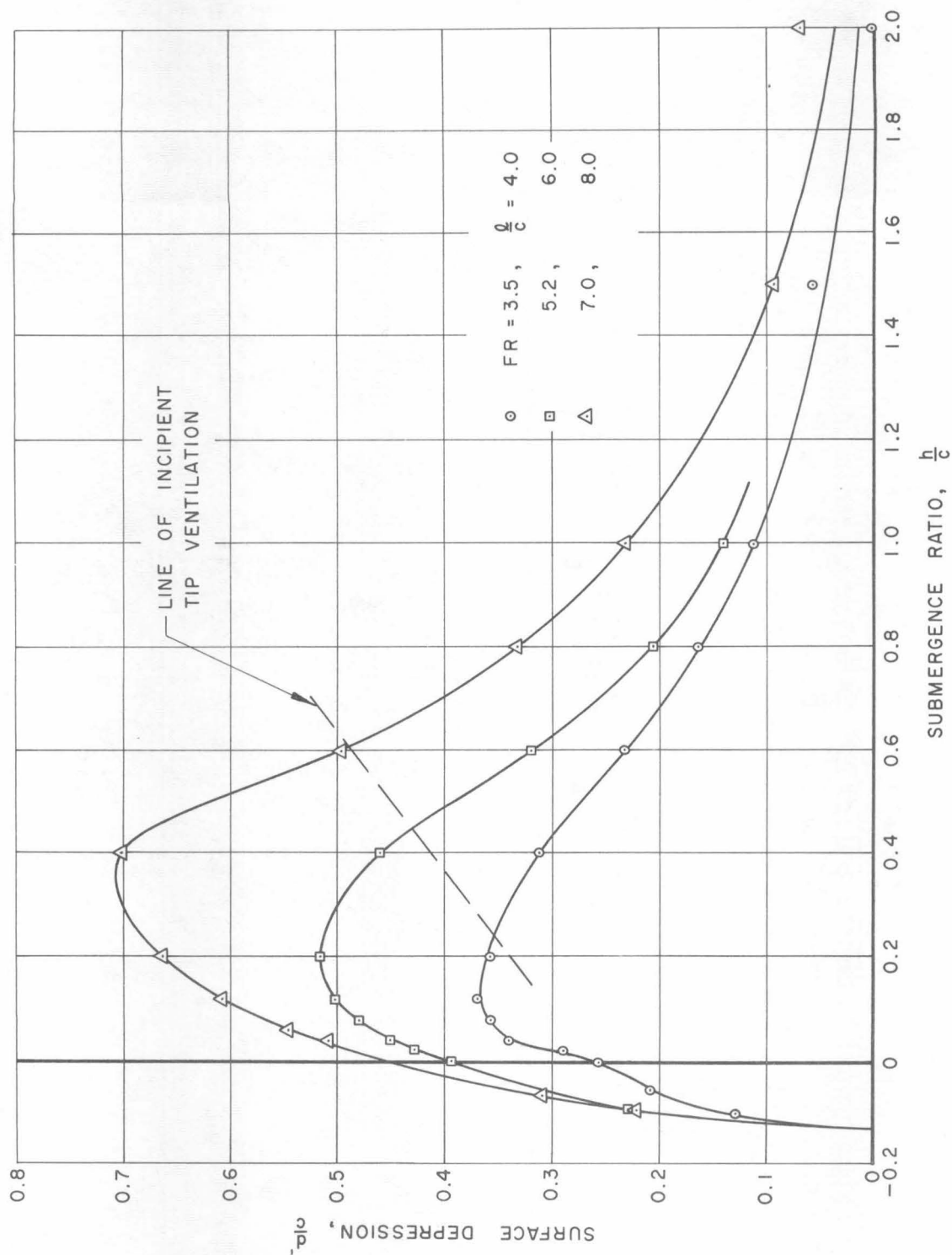


Figure 9. Maximum surface depression behind hydrofoil as a function of submergence and Froude number. The angle of attack is  $8^\circ$  and the aspect ratio of the hydrofoil is  $4/3$ .

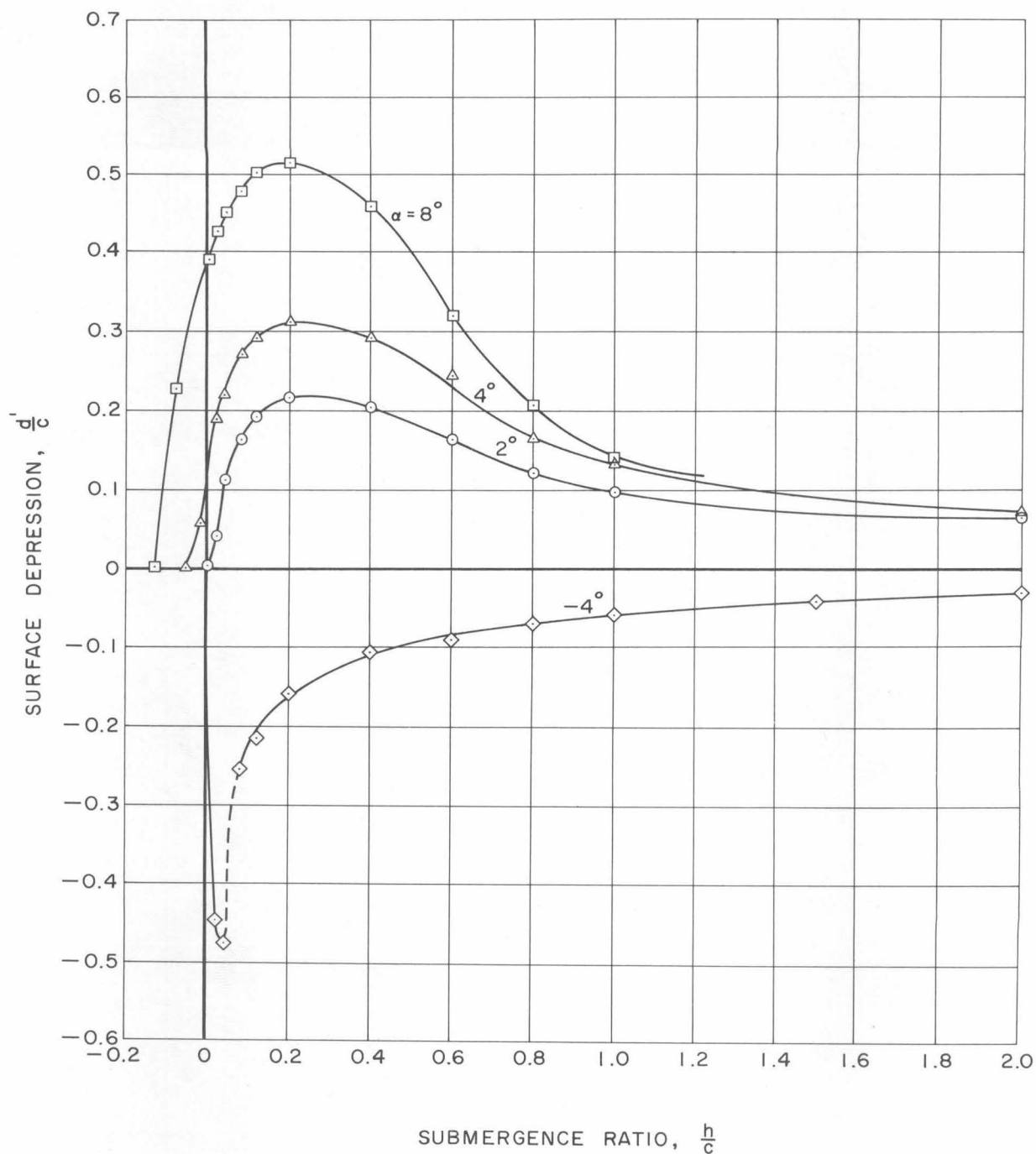


Figure 10. Maximum surface depression behind hydrofoil as a function of submergence ratio and angle of attack. The Froude number is 5.28 (based on chord) for all angles. The aspect ratio of the hydrofoil is 4/3.

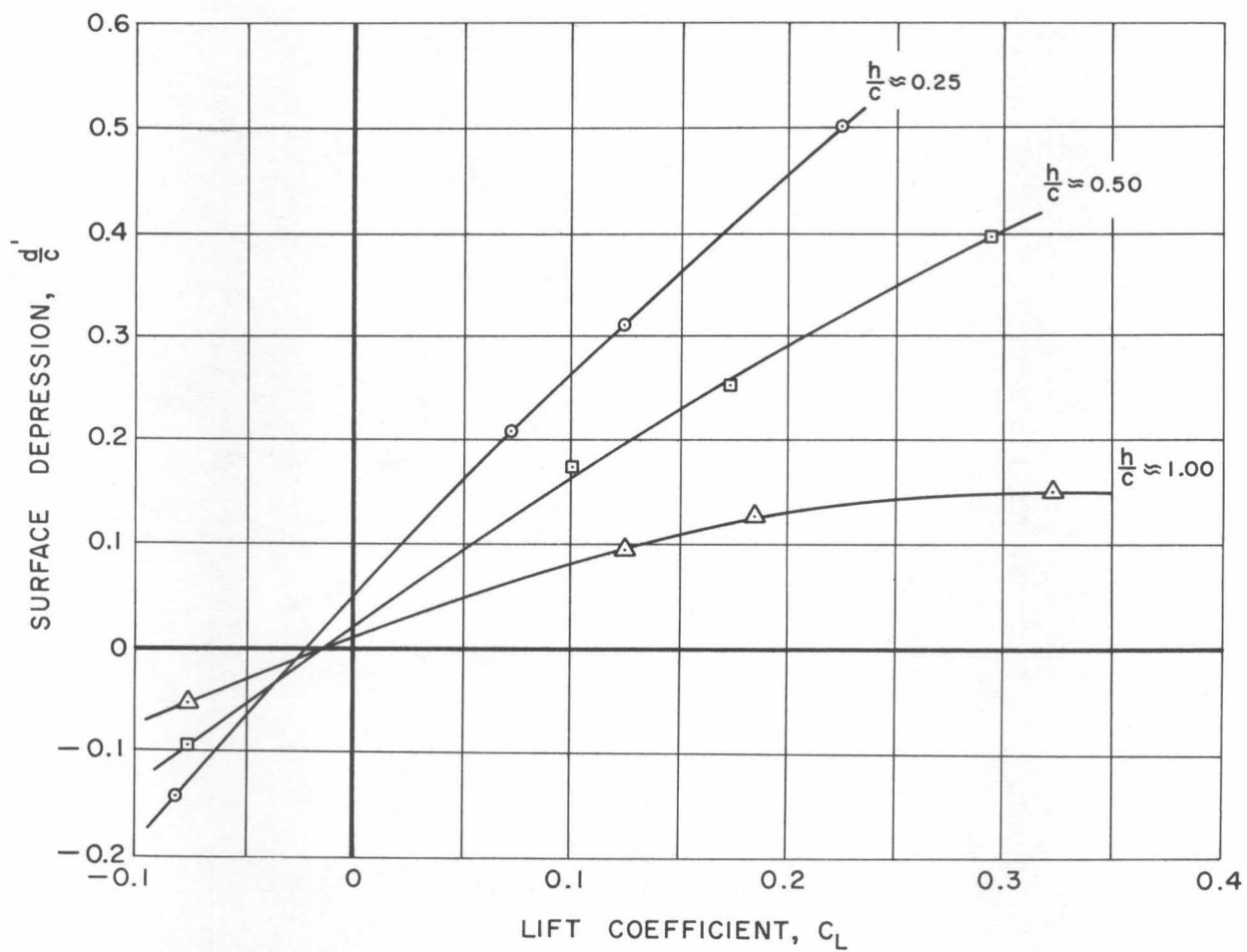


Figure 11. Maximum surface depression as a function of depth and lift coefficient for a Froude number of 5.3 (based on chord). The aspect ratio is 4/3.

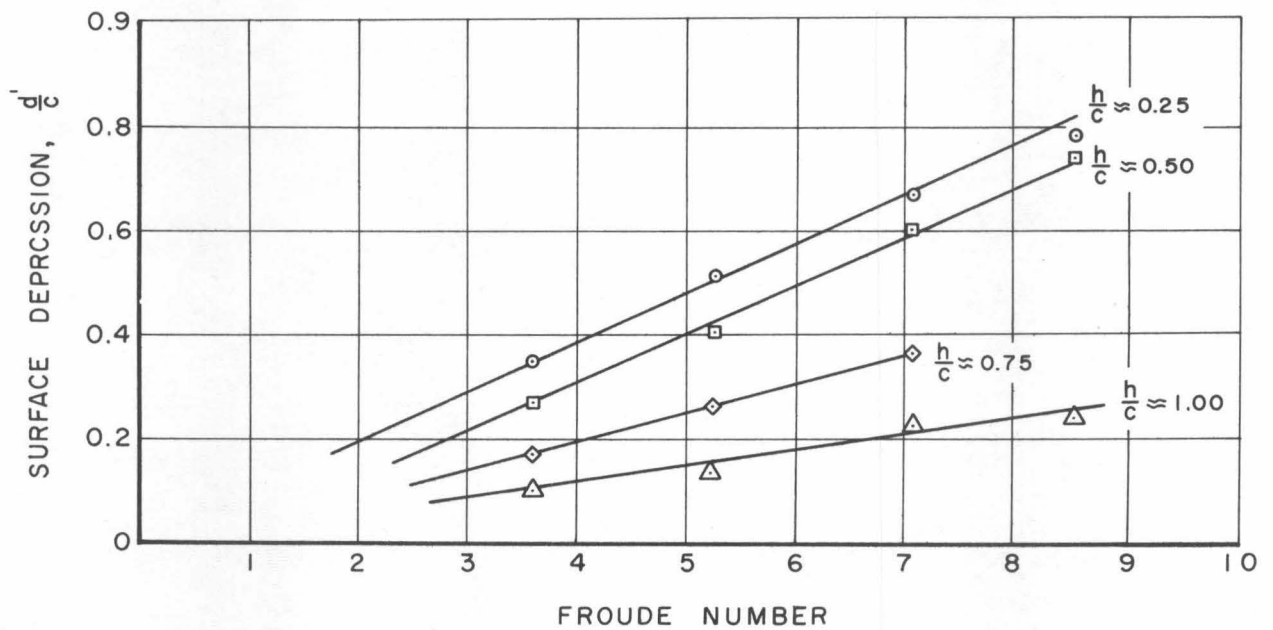


Figure 12. Maximum surface depression as a function of Froude number and submergence ratio.

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